

Question	Scheme	Marks	AOs
1 (a)	$3x^3 - 17x^2 - 6x = 0 \Rightarrow x(3x^2 - 17x - 6) = 0$	M1	1.1a
	$\Rightarrow x(3x+1)(x-6) = 0$	dM1	1.1b
	$\Rightarrow x = 0, -\frac{1}{3}, 6$	A1	1.1b
		(3)	
(b)	Attempts to solve $(y-2)^2 = n$ where n is any solution ...0 to (a)	M1	2.2a
	Two of $2, 2 \pm \sqrt{6}$	A1ft	1.1b
	All three of $2, 2 \pm \sqrt{6}$	A1	2.1
		(3)	

(6 marks)

Notes

(a)

M1: Factorises out or cancels by x to form a quadratic equation.

dM1: Scored for an attempt to find x . May be awarded for factorisation of the quadratic or use of the quadratic formula.

A1: $x = 0, -\frac{1}{3}, 6$ and no extras

(b)

M1: Attempts to solve $(y-2)^2 = n$ where n is any solution ...0 to (a). At least one stage of working must be seen to award this mark. Eg $(y-2)^2 = 0 \Rightarrow y = 2$

A1ft: Two of $2, 2 \pm \sqrt{6}$ but follow through on $(y-2)^2 = n \Rightarrow y = 2 \pm \sqrt{n}$ where n is a positive solution to part (a). (Provided M1 has been scored)

A1: All three of $2, 2 \pm \sqrt{6}$ and no extra solutions. (Provided M1A1 has been scored)

Question	Scheme	Marks	AOs
2 (a)	Deduces the line has gradient "-3" and point (7,4) Eg $y - 4 = -3(x - 7)$	M1	2.2a
	$y = -3x + 25$	A1	1.1b
	(2)		
(b)	Solves $y = -3x + 25$ and $y = \frac{1}{3}x$ simultaneously	M1	3.1a
	$P = \left(\frac{15}{2}, \frac{5}{2}\right)$ oe	A1	1.1b
	Length $PN = \sqrt{\left(\frac{15}{2} - 7\right)^2 + \left(4 - \frac{5}{2}\right)^2} = \left(\sqrt{\frac{5}{2}}\right)$	M1	1.1b
	Equation of C is $(x - 7)^2 + (y - 4)^2 = \frac{5}{2}$ o.e.	A1	1.1b
	(4)		
(c)	Attempts to find where $y = \frac{1}{3}x + k$ meets C using vectors Eg: $\begin{pmatrix} 7.5 \\ 2.5 \end{pmatrix} + 2 \times \begin{pmatrix} -0.5 \\ 1.5 \end{pmatrix}$	M1	3.1a
	Substitutes their $\left(\frac{13}{2}, \frac{11}{2}\right)$ in $y = \frac{1}{3}x + k$ to find k	M1	2.1
	$k = \frac{10}{3}$	A1	1.1b
	(3)		
(9 marks)			
(c)	Attempts to find where $y = \frac{1}{3}x + k$ meets C via simultaneous equations proceeding to a 3TQ in x (or y) FYI $\frac{10}{9}x^2 + \left(\frac{2}{3}k - \frac{50}{3}\right)x + k^2 - 8k + \frac{125}{2} = 0$	M1	3.1a
	Uses $b^2 - 4ac = 0$ oe and proceeds to $k = \dots$	M1	2.1
	$k = \frac{10}{3}$	A1	1.1b
	(3)		

Notes:

(a)

M1: Uses the idea of perpendicular gradients to deduce that gradient of PN is -3 with point $(7,4)$ to find the equation of line PN

So sight of $y - 4 = -3(x - 7)$ would score this mark

If the form $y = mx + c$ is used expect the candidates to proceed as far as $c = \dots$ to score this mark.

A1: Achieves $y = -3x + 25$

(b)

M1: Awarded for an attempt at the key step of finding the coordinates of point P . ie for an attempt at solving their $y = -3x + 25$ and $y = \frac{1}{3}x$ simultaneously. Allow any methods (including use of a calculator) but it must be a valid attempt to find both coordinates.

A1: $P = \left(\frac{15}{2}, \frac{5}{2}\right)$

M1: Uses Pythagoras' Theorem to find the radius or radius ² using their $P = \left(\frac{15}{2}, \frac{5}{2}\right)$ and $(7, 4)$.

There must be an attempt to find the difference between the coordinates in the use of Pythagoras

A1: Full and careful work leading to a correct equation. Eg $(x-7)^2 + (y-4)^2 = \frac{5}{2}$ or its expanded

form. Do not accept $(x-7)^2 + (y-4)^2 = \left(\sqrt{\frac{5}{2}}\right)^2$

(c)

M1: Attempts to find where $y = \frac{1}{3}x + k$ meets C using a vector approach

M1: For a full method leading to k . Scored for substituting their $\left(\frac{13}{2}, \frac{11}{2}\right)$ in $y = \frac{1}{3}x + k$

A1: $k = \frac{10}{3}$ only

Alternative I

M1: For solving $y = \frac{1}{3}x + k$ with their $(x-7)^2 + (y-4)^2 = \frac{5}{2}$ and creating a quadratic eqn of the form $ax^2 + bx + c = 0$ **where both b and c are dependent upon k** . The terms in x^2 and x must be collected together or implied to have been collected by their correct use in " $b^2 - 4ac$ "

FYI the correct quadratic is $\frac{10}{9}x^2 + \left(\frac{2}{3}k - \frac{50}{3}\right)x + k^2 - 8k + \frac{125}{2} = 0$ oe

M1: For using the discriminant condition $b^2 - 4ac = 0$ to find k . It is not dependent upon the previous M and may be awarded from only one term in k .

Award if you see use of correct formula but it would be implied by \pm correct roots

A1: $k = \frac{10}{3}$ only

Alternative II

M1: For solving $y = -3x + 25$ with their $(x-7)^2 + (y-4)^2 = \frac{5}{2}$, creating a 3TQ and solving.

M1: For substituting their $\left(\frac{13}{2}, \frac{11}{2}\right)$ into $y = \frac{1}{3}x + k$ and finding k

A1: $k = \frac{10}{3}$ only

Question	Scheme	Marks	AOs
3(a)	$f(-3) = 2(-3)^3 + 5(-3)^2 + 2(-3) + 15$ $= -54 + 45 - 6 + 15$	M1	1.1b
	$f(-3) = 0 \Rightarrow (x + 3)$ is a factor	A1	2.4
		(2)	
(b)	At least 2 of: $a = 2, b = -1, c = 5$	M1	1.1b
	All of: $a = 2, b = -1, c = 5$	A1	1.1b
		(2)	
(c)	$b^2 - 4ac = (-1)^2 - 4(2)(5)$	M1	2.1
	$b^2 - 4ac = -39$ which is < 0 so the quadratic has no real roots so $f(x) = 0$ has only 1 real root	A1	2.4
		(2)	
(d)	$(x =) 2$	B1	2.2a
		(1)	

(7 marks)

Notes

(a)

M1: Attempts $f(-3)$. Attempted division by $(x + 3)$ or $f(3)$ is M0
Look for evidence of embedded values or two correct terms of
 $f(-3) = -54 + 45 - 6 + 15 = \dots$

A1: Achieves and states $f(-3) = 0$, and makes a suitable conclusion. Sight of $f(x) = 0$ when
 $x = -3$ is also acceptable.
It must follow M1. Accept, for example, $f(-3) = 0 \Rightarrow (x + 3)$ is a factor

This may be seen in a preamble before finding $f(-3) = 0$ but in these cases there must be a minimal statement ie QED, "proved", tick etc.

(b)

M1: Correct method implied by values for at least 2 correct constants. Allow embedded in their $f(x)$ or within their working if they use algebraic division/other methods which may be seen in part (a) and used in part (b).

A1: All values correct. Allow embedded in their $f(x)$ or seen as the quotient from algebraic division. Isw incorrectly stated values of a b and c following a correct quadratic expression seen.

$$\begin{array}{r}
 \overline{2x^2 - x + 5} \\
 x+3 \overline{) 2x^3 + 5x^2 + 2x + 15} \\
 \underline{2x^3 + 6x^2} \\
 -x^2 + 2x \\
 \underline{ -x^2 - 3x} \quad \text{scores M1A1} \\
 5x + 15 \\
 \underline{ 5x + 15} \\
 0
 \end{array}$$

(c)

M1: Either:

- considers the discriminant using their a , b and c (does not need to be evaluated) $(b^2 - 4ac =) (-1)^2 - 4(2)(5)$ (the $(-1)^2$ may appear as 1^2 and condone missing brackets for this mark for -1^2). Discriminant = -39 is sufficient for M1
- attempts to complete the square so score for $2\left(x \pm \frac{1}{4}\right)^2 + \dots$
- attempts to find the roots of the quadratic using the formula. The values embedded in the formula score this mark.

$$\frac{1 \pm \sqrt{(-1)^2 - 4 \times 2 \times 5}}{2 \times 2}$$
 (the $(-1)^2$ may appear as 1^2 and condone missing brackets for this mark for -1^2)
- Sketches a graph of the quadratic. It must be a U shaped quadratic which does not cross the x -axis.

A1: Provides a correct explanation from correct working. They must

- Have a correct calculation
- Explanation that the quadratic has no (real) roots
- Minimal conclusion stating that $f(x) = 0$ has only one root

eg $b^2 - 4ac = -39 < 0$ so only one root is M1A0 (needs to explain the quadratic has no real roots)

eg $2\left(x - \frac{1}{4}\right)^2 + \frac{39}{8} > 0$ **so no real roots** (for the quadratic) **so** ($f(x)$ has) **only one** (real) **root** is M1A1

The value of the discriminant, completed square form $2\left(x - \frac{1}{4}\right)^2 + \frac{39}{8}$ or roots of the

quadratic $\left(= \frac{1 \pm \sqrt{39i}}{4}\right)$ must be correct.

If they sketch the quadratic graph it must be a U shaped quadratic which crosses the y -axis at 5 and has a minimum in the 1st quadrant. They must explain that the graph does not cross the x -axis so no real roots for the quadratic so only one root for $f(x) = 0$.

(d)

B1: 2 condone (2, 0)

Question	Scheme	Marks	AOs
4	Let $u = \sqrt{x}$ $6x + 7\sqrt{x} - 20 = 0 \Rightarrow 6u^2 + 7u - 20 = 0$ $\Rightarrow (3u - 4)(2u + 5) = 0$	M1A1	1.1b 1.1b
	Attempts $\sqrt{x} = \frac{4}{3}, -\frac{5}{2} \Rightarrow x = \dots$	M1	1.1b
	$x = \frac{16}{9}$ only	A1 cso	2.3
		(4)	

(4 marks)

Alt 1	$6x + 7\sqrt{x} - 20 = 0 \Rightarrow 7\sqrt{x} = 20 - 6x \Rightarrow 49x = (20 - 6x)^2$ $\Rightarrow 49x = 400 - 240x + 36x^2$	M1	1.1b
	$36x^2 - 289x + 400 = 0$	A1	1.1b
	$(9x - 16)(4x - 25) = 0$	M1	1.1b
	$x = \frac{16}{9}$ only	A1 cso	2.3

(4)

Alt 2	$6x + 7\sqrt{x} - 20 = 0 \Rightarrow (3\sqrt{x} - 4)(2\sqrt{x} + 5) = 0$	M1 A1	1.1b 1.1b
	Attempts $\sqrt{x} = \frac{4}{3}, -\frac{5}{2} \Rightarrow x = \dots$	M1	1.1b
	$x = \frac{16}{9}$ only	A1 cso	2.3
		(4)	

Notes:

M1: Attempts a valid method that enables the problem to be solved. See General Principles for Pure Mathematics Marking at the front of the mark scheme for guidance. Score for either letting $u = \sqrt{x}$ and attempting to factorise to $(au \pm c)(bu \pm d)$ with $ab = 6, cd = 20$

or making $7\sqrt{x}$ the subject and attempting to square both sides.

or attempting to factorise to $(a\sqrt{x} \pm c)(b\sqrt{x} \pm d)$ with $ab = 6, cd = 20$

or by quadratic formula or completing the square following usual rules.

A1: $(3u - 4)(2u + 5) = 0$ or $36x^2 - 289x + 400 = 0$ or $(3\sqrt{x} - 4)(2\sqrt{x} + 5) = 0$

If they use the formula, it must be correct e.g., $u \text{ {or } } \sqrt{x} = \frac{-7 \pm \sqrt{7^2 - 4(6)(-20)}}{12}$ followed

by $u \text{ {or } } \sqrt{x} = \frac{4}{3}$ or equivalent e.g., $\frac{16}{9}$. Ignore if they have $u \text{ {or } } \sqrt{x} = -\frac{5}{2}$ or not.

If they complete the square, they must have $\left(u + \frac{7}{12}\right)^2 = \frac{529}{144}$ followed by u {or \sqrt{x} } = $\frac{4}{3}$ or equivalent e.g., $\frac{16}{12}$. Ignore if they have u {or \sqrt{x} } = $-\frac{5}{2}$ or not.

M1: Correct method from $p\sqrt{x} \pm q = 0$ leading to $x = \dots$ by squaring

In Alt 1, it is for solving their quadratic using the General Principles for Pure Mathematics Marking. There must be a method shown, i.e., the solutions should not come straight from a calculator. If attempting to factorise, it must be to $(ax \pm c)(bx \pm d)$ with $ab = 36, cd = 400$

In Alt 2, it is for squaring their value(s) for u to get $x = \dots$

A1: **cs0** $x = \frac{16}{9}$ only. $x = \frac{25}{4}$ must be discarded. Note 0011 is not possible.

Allow “incorrect” $x = -\frac{16}{9}$ or $x = -\frac{25}{4}$ to be seen as long as they are discarded.

Ignore any reason they give for rejecting solutions.

Note that a method to solve their quadratic must be seen – solutions must not come directly from a calculator. Simply stating the quadratic formula (without substitution) is insufficient.

Question	Scheme	Marks	AOs
5 (a)	Attempts both $y = 8 - 10 \times 1 + 6 \times 1^2 - 1^3$ and $y = 1^2 - 12 \times 1 + 14$	M1	1.1b
	Achieves $y = 3$ for both equations and gives a minimal conclusion / statement, e.g., $(1, 3)$ lies on both curves so they intersect at $x = 1$	A1	1.1b
		(2)	
(b)	(Curves intersect when) $x^2 - 12x + 14 = 8 - 10x + 6x^2 - x^3$ $\Rightarrow x^3 - 5x^2 - 2x + 6 = 0$	M1	1.1b
	For the key step in dividing by $(x - 1)$ $x^3 - 5x^2 - 2x + 6 = (x - 1)(x^2 + px \pm 6)$	dM1	3.1a
	$x^3 - 5x^2 - 2x + 6 = (x - 1)(x^2 - 4x - 6)$	A1	1.1b
	Solves $x^2 - 4x - 6 = 0$ $(x - 2)^2 = 10 \Rightarrow x = \dots$	ddM1	1.1b
	$x = 2 - \sqrt{10}$ only	A1	1.1b
		(5)	

(7 marks)

Notes:

(a) Must be seen in (a)

M1: As scheme.

For M1 A0, allow a statement that $(1, 3)$ lies on both curves without sight of the calculation.

Amongst various alternatives are:

- Setting $x^2 - 12x + 14 = 8 - 10x + 6x^2 - x^3$ and attempting to rearrange to $x^3 - 5x^2 - 2x + 6 = 0$ before substituting in $x = 1$
- Setting $x^2 - 12x + 14 = 8 - 10x + 6x^2 - x^3$ and attempting to divide $x^3 - 5x^2 - 2x + 6$ by $(x - 1)$ either by long division or inspection

A1: For the complete mathematical argument.

Requires both correct calculations with a minimal conclusion, which may be as a preamble. e.g., in the alternatives

- as $1^3 - 5 \times 1^2 - 2 \times 1 + 6 = 0$, hence curves meet when $x = 1$
- $x^3 - 5x^2 - 2x + 6 = (x - 1)(x^2 - 4x - 6)$ so the curves intersect when $x = 1$

(b) Allow the use of x or k throughout this part.

M1: Sets $x^2 - 12x + 14 = 8 - 10x + 6x^2 - x^3$ and proceeds to a cubic equation set = 0
Must be seen or used in (b)

dM1: For the key step in realising that $(x - 1)$ is a factor of the cubic.
It is for dividing by $(x - 1)$ to get the quadratic factor.

For division look for their first two terms, i.e., $x^2 \pm 4x$

(This will need checking if they have made an error in rearranging the cubic.)

$$\begin{array}{r} x^2 \pm 4x \dots\dots\dots \\ x-1 \overline{) x^3 - 5x^2 - 2x + 6} \\ \underline{x^3 - 1x^2} \\ -4x^2 \end{array}$$

By inspection look for the first and last term $x^3 - 5x^2 - 2x + 6 = (x-1)(x^2 + px \pm 6)$

A1: $x^3 - 5x^2 - 2x + 6 = (x-1)(x^2 - 4x - 6)$ or just $x^2 - 4x - 6$ or $k^2 - 4k - 6$ as their quadratic factor following algebraic division.

ddM1: Attempts to solve their $x^2 - 4x - 6 = 0$, which must be a 3TQ, by completing the square or the quadratic formula, leading to an exact solution. Their quadratic factor must **not** factorise. Their quadratic “factor” may come from algebraic division that has a remainder but we will still allow them to score this mark.

If using the quadratic formula, they need to have, e.g., $\frac{4 - \sqrt{4^2 - 4(-6)}}{2}$

or $\frac{4 - \sqrt{40}}{2}$ as a minimum (i.e., they must not jump straight to $2 - \sqrt{10}$ from a calculator).

A1: $k = 2 - \sqrt{10}$ or exact equivalent but allow the use of x e.g., $x = \frac{4 - \sqrt{40}}{2}$

If using the quadratic formula, the discriminant must be processed.

Must come from a correct quadratic factor.

They must have discarded $2 + \sqrt{10}$ if seen.

Question	Scheme	Marks	AOs
6(a)	$f(x) = (x-2)^2 \pm \dots$	M1	1.2
	$f(x) = (x-2)^2 + 1$	A1	1.1b
		(2)	
(b)(i)	$P = (0, 5)$	B1	1.1b
(b)(ii)	$Q = (2, 1)$	B1ft	1.1b
		(2)	
(4 marks)			
Notes			

(a)

M1: Achieves $(x-2)^2 \pm \dots$ or states $a = -2$

A1: Correct expression $(x-2)^2 + 1$ ISW after sight of this

Condone $a = -2$ and $b = 1$. Condone $(x-2)^2 + 1 = 0$

(b)

(i) B1: Correct coordinates for P . Allow to be expressed $x = 0, y = 5$

(ii) B1ft: Correct coordinates for Q . Allow to be expressed $x = 2, y = 1$ (Score for the correct answer or follow through their part (a) so allow $(-a, b)$ where a and b are numeric)

Score in any order if they state $P = (0, 5)$ and $Q = (2, 1)$

.....
 Allow part (b) to be awarded from a sketch. So award

First B1 from a sketch crossing the y -axis at 5

Second B1 from a sketch with minimum at $(2, 1)$

Question	Scheme	Marks	AOs
7(a)	$H = ax^2 + bx + c$ and $x=0, H=3 \Rightarrow H = ax^2 + bx + 3$	M1	3.3
	$H = ax^2 + bx + 3$ and $x = 120, H = 27 \Rightarrow 27 = 14400a + 120b + 3$	M1	3.1b
	or $\frac{dH}{dx} = 2ax + b = 0$ when $x = 90 \Rightarrow 180a + b = 0$	A1	1.1b
	$H = ax^2 + bx + 3$ and $x = 120, H = 27 \Rightarrow 27 = 14400a + 120b + 3$ and $\frac{dH}{dx} = 2ax + b = 0$ when $x = 90 \Rightarrow 180a + b = 0$ $\Rightarrow a = \dots, b = \dots$	dM1	3.1b
	$H = -\frac{1}{300}x^2 + \frac{3}{5}x + 3$ o.e.	A1	1.1b
		(5)	
(b)(i)	$x = 90 \Rightarrow H \left(= -\frac{1}{300}(90)^2 + \frac{3}{5}(90) + 3 \right) = 30 \text{ m}$	B1	3.4
(b)(ii)	$H = 0 \Rightarrow -\frac{1}{300}x^2 + \frac{3}{5}x + 3 = 0 \Rightarrow x = \dots$	M1	3.4
	$x = (-4.868\dots), 184.868\dots$ $\Rightarrow x = 185 \text{ (m)}$	A1	3.2a
		(3)	
(c)	Examples must focus on why the model may not be appropriate or give values/situations where the model would break down: E.g. <ul style="list-style-type: none"> The ground is unlikely to be horizontal The ball is not a particle so has dimensions/size The ball is unlikely to travel in a vertical plane (as it will spin) H is not likely to be a quadratic function in x 	B1	3.5b
		(1)	
			(9 marks)
Notes			

(a)

M1: Translates the problem into a suitable model and uses $H = 3$ when $x = 0$ to establish $c = 3$

Condone with $a = \pm 1$ so $H = x^2 + bx + 3$ will score M1 but little else

M1: For a correct attempt at **using one of the two other pieces** of information within a quadratic model

Either uses $H = 27$ when $x = 120$ (with $c = 3$) to produce a linear equation connecting a and b for

the model **Or** differentiates and uses $\frac{dH}{dx} = 0$ when $x = 90$. Alternatives exist here, using the

symmetrical nature of the curve, so they could use $x = -\frac{b}{2a}$ at vertex or use point $(60, 27)$ or $(180, 3)$.

A1: At least one correct equation connecting a and b . Remember " a " could have been set as negative so an equation such as $27 = -14400a + 120b + 3$ would be correct in these circumstances.

dM1: Fully correct strategy that uses $H = ax^2 + bx + 3$ with the two other pieces of information in order to establish the values of **both a and b** for the model

A1: Correct equation, not just the correct values of a, b and c . Award if seen in part (b)

(b)(i)

B1: Correct height including the units. CAO

(b)(ii)

M1: Uses $H = 0$ and attempts to solve for x . Usual rules for quadratics.

A1: Discards the negative solution (may not be seen) and identifies awrt 185 m. Condone lack of units

(c)

B1: Candidate should either refer to an issue with one of the four aspects of how the situation has been modelled or give a situation where the model breaks down

- the ball has been modelled as a particle
- there may be trees (or other hazards) in the way that would affect the motion

Condone answers (where the link to the model is not completely made) such as

- the ball will spin
- ground is not flat

Do not accept answers which refer to the situation after it hits the ground (this isn't what was modelled)

- the ball will bounce after hitting the ground
- it gives a negative height for some values for x

Do not accept answers that do not refer to the model in question, or else give single word vague answers

- the height of tee may have been measured incorrectly
- "friction", "spin", "force" etc
- it does not take into account the weight of the ball
- it depends on how good the golfer is
- the shape of the ball will affect the motion
- you cannot hit a ball the same distance each time you hit it

The method using an alternative form of the equation can be scored in a very similar way.

The first M is for the completed square form of the quadratic showing a maximum at $x = 90$

So award M1 for $H = \pm a(x-90)^2 + c$ or $H = \pm a(90-x)^2 + c$. Condone for this mark an equation with

$a = 1 \Rightarrow H = (x-90)^2 + c$ or $c = 3 \Rightarrow H = a(x-90)^2 + 3$ but will score little else

Alt (a)	$H = a(x+b)^2 + c$ and $x=90$ at $H_{\max} \Rightarrow H = a(x-90)^2 + c$	M1	3.3
	$H = 3$ when $x = 0 \Rightarrow 3 = 8100a + c$ or $H = 27$ when $x = 120 \Rightarrow 27 = 900a + c$	M1 A1	3.1b 1.1b
	$H = 3$ when $x = 0 \Rightarrow 3 = 8100a + c$ and $H = 27$ when $x = 120 \Rightarrow 27 = 900a + c$ $\Rightarrow a = \dots, c = \dots$	dM1	3.1b
	$H = -\frac{1}{300}(x-90)^2 + 30$ o.e	A1	1.1b
		(5)	
(b)	$x = 90 \Rightarrow H = 0^2 + 30 = 30$ m	B1	3.4
		(1)	
	$H = 0 \Rightarrow 0 = -\frac{1}{300}(x-90)^2 + 30 \Rightarrow x = \dots$	M1	3.4
	$\Rightarrow x = 185$ (m)	A1	3.2a
		(2)	

Note that $H = -\frac{1}{300}(x-90)^2 + 30$ is equivalent to $H = -\frac{1}{300}(90-x)^2 + 30$

Other versions using symmetry are also correct so please look carefully at all responses

E.g. Using a starting equation of $H = a(x-60)(x-120) + b$ leads to $H = -\frac{1}{300}(x-60)(x-120) + 27$

Question	Scheme	Marks	AOs
8(a)	$a = 60$	B1	3.1b
	$2 = "60" - b(-20)^2 \Rightarrow b = \dots$	M1	3.4
	$H = 60 - 0.145(t - 20)^2$	A1	3.3
		(3)	
(b)	Height = 2 m	B1	3.4
		(1)	
(c)	$\alpha = 180$ or $\beta = 31$	M1	3.4
	$H = 29 \cos(9t + 180)^\circ + 31$	A1	3.3
		(2)	
(d)	e.g. "The model allows for more than one circuit"	B1	3.5a
		(1)	

(7 marks)

Notes

(a)	<p>B1: $a = 60$ (may be seen in their final equation of the model or implied by 60 substituted for a in the model)</p> <p>M1: Attempts to find b by substituting in $t = 0$, $H = 2$ and their a and proceeding to a value for b. May be seen as two simultaneous equations formed: $2 = a - b(-20)^2$ and $60 = a - b(20 - 20)^2$ proceeding to a value for b</p> <p>A1: $H = 60 - 0.145(t - 20)^2$ or equivalent such as $H = -\frac{29}{200}t^2 + 5.8t + 2$ or $H = 60 - \frac{29}{200}(t - 20)^2$ isw once a correct equation for the model is seen. Must be in terms of H and t. If they just state $a = 60$, $b = 0.145$ then A0 A correct answer with no working seen scores full marks.</p>																																		
(b)	<p>B1: 2 cao (condone lack of units) This can be scored even if their model in (a) is incorrect (they may have used symmetry to determine this value)</p>																																		
(c)	<p>M1: $(\alpha =) 180$ or $(\beta =) 31$ Condone $(\alpha =) \pi$</p> <p>A1: $H = 29 \cos(9t + 180)^\circ + 31$ or equivalent e.g. $H = -29 \cos(9t) + 31$ isw once a correct equation for the model is seen. Must be in terms of H and t. If they just state $\alpha = 180$, $\beta = 31$ then A0. A correct equation with no working seen scores both marks. Does not require the degree symbol.</p>																																		
(d)	<p>B1: Score for a reason which makes reference to any of</p> <ul style="list-style-type: none"> the alternative model allows repetition (allow phrases e.g. "multiple cycles", "repeated circuits", "cyclical", "periodic", "loops around", "the original model can only go up and down once") the alternative model after 2 minutes the carriage will be back at the start (e.g. "at 2 mins, $H = 2$") the original/quadratic model after 40 seconds (or any time after this) will be negative (e.g. "the height will be negative which cannot happen") the original model after 2 minutes would not be back at the start <p>Do not allow vague responses on their own e.g. "the original model is a parabola" If calculations are used then they must be correct using a correct model (allow rounded or truncated) Look for a valid reason and ignore reference to anything else as long as it does not contradict</p> <table border="1"> <tbody> <tr> <td>t</td> <td>0</td> <td>5</td> <td>10</td> <td>15</td> <td>20</td> <td>25</td> <td>30</td> <td>35</td> <td>40</td> <td>45</td> <td>50</td> <td>55</td> <td>60</td> <td>80</td> <td>100</td> <td>120</td> </tr> <tr> <td>h</td> <td>2</td> <td>27</td> <td>46</td> <td>56</td> <td>60</td> <td>56</td> <td>46</td> <td>27</td> <td>2</td> <td>-31</td> <td>-71</td> <td>-118</td> <td>-172</td> <td>-462</td> <td>-868</td> <td>-1390</td> </tr> </tbody> </table>	t	0	5	10	15	20	25	30	35	40	45	50	55	60	80	100	120	h	2	27	46	56	60	56	46	27	2	-31	-71	-118	-172	-462	-868	-1390
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